

8/9/21

Maths

1) Without actual multiplication:

$$(103)^2 \\ = (10,609) \text{ actual value.}$$

2) Factorise the following

$$16m^2 - 9n^2 \\ = 16m^2 - 9n^2 \\ = \cancel{16m^2} \\ = 206m - 81n \\ = \underline{125mn}$$

$$3) (3x+4y)^2 = (3x)^2 + 2 \times 3x \times 4y + (4y)^2 \\ = 9x^2 + 24xy + 16$$

$$4) \left[\frac{x}{2} - \frac{y}{3} \right]^2 \\ = \left(\frac{x}{2} \right)^2 + 2 \times \frac{x}{2} \times \frac{y}{3} + \left(\frac{y}{3} \right)^2 \\ = \frac{x^2}{4} + \frac{2xy}{3} + \frac{y^2}{9}$$

$$5) (a^2b - b^2a)^2 \\ = [ab(a-b)]^2 \\ = (ab)^2 (a-b)^2 \\ = (ab)^2 (a^2 - 2ab + b^2) \\ = a^2b^2 (a^2 - 2ab + b^2) \\ = a^4b^2 - 2a^3b^3 + a^2b^4$$

$$6) (1.5x^2 - 0.3y^2)(1.5x^2 + 0.3y^2)$$

$$(a-b)(a+b) = a^2 - b^2$$

$$(1.5x^2)^2 - (0.3y^2)^2 \\ = 2.25x^4 - 0.09y^4$$

$$\underline{7} \quad 9x^2 + 25y^2 = 181$$

$$xy = -6$$

$$(3x+5y)^2 = 9x^2 + 25y^2 + 2 \times 3x \times 5y$$

$$= 9x^2 + 25y^2 + 30xy$$

$$= 181 + 30(-6)$$

$$= 181 - 180$$

$$= 1$$

8) Evaluate the 104×96

$$= 104 \times 96$$

$$= (100+4)(100-4)$$

$$= (x+y)(x-y) = x^2 - y^2$$

$$x=100, y=4$$

$$= (100)^2 - (4)^2$$

$$= 10000 - 16$$

$$= 9984$$

9) $(997)^2$

$$= (1000-3)^2$$

$$= (1000)^2 + 3^2$$

$$- 2(1000) \times 3$$

$$= 1000000 + 9 - 6000$$

$$= 994,009$$

10) 103×107

$$= (100+3)(100+7)$$

$$(x+a)(x+b) = x^2 + (a+b)x + ab$$

$$x=100, a=3, b=7$$

$$= (100)^2 + (3+7)100 + (3)(7)$$

$$= 10000 + (10)(100) + 21$$

$$= 10000 + 1000 + 21$$

$$= 11021$$

12) Evaluate using identities

$$2.07 \times 1.93$$

$$= (2+0.07)(2-0.07)$$

$$= 2^2 - 0.07^2$$

$$= 4 - 0.0049$$

$$= 3.9951$$